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## LETTERS TO THE EDITORS

## COMMENTS ON 'MATHEMATICAL MODELLING OF BUOYANCY-INDUCED SMOKE FLOW IN ENCLOSURES'

I HAVE read the Paper of Markatos et al. [1] where a buoyancy affected  $k \sim \varepsilon$  model of turbulence has been used for the prediction of buoyancy-induced flows in enclosures. Buoyancy affected  $k \sim \varepsilon$  turbulence models have already been successfully used to calculate both vertical and horizontal shear layer flows  $[2,3]$  but so far as I know this is one of the first attempts to predict recirculating flows with it.

The authors have introduced the influence of buoyancy only in the generation terms of the equations of  $k$  and  $\varepsilon$ , neglecting its influence in the expression of turbulent viscosity  $\mu_{\rm t}$  (equation (9) in ref. [1]), and in the constants  $\sigma_{\rm t}$  (turbulent Prandtl number),  $\sigma_k$  and  $\sigma_r$ . The authors however did not mention the value of  $\sigma_t$  used in their calculations.

For the introduction of buoyancy in the equation of *k* no further empirical information is necessary whereas its introduction in the  $\varepsilon$ -equation is a very sensible issue because the e-equation without the buoyancy effect contains already two very sensitive empirical constants  $C_1$  and  $C_2$ . The authors have also discussed this problem in details mentioning about the solution proposals but it is not clear to me exactly which approach has been finally used in their calculations.

It appears they have used the proposal of Rodi [4] which uses a single value of  $C_3$  for use in the vertical and horizontal shear layers but requires different values of the buoyancy production of the lateral energy component  $G_{BL}$  (equation  $(18)$  in ref.  $[1]$ ) which has a meaning only in the case of shear layer flows as has been used in refs.  $[2]$  and  $[3]$ .

Thus the authors have either used the horizontal shear layer approach,  $G_{BL} = 2 \cdot G_B$  with  $C_3$  influence in it or vertical shear layer approach,  $G_{BL} = 0$  for which the influence of  $C_3$ automatically disappears.

In Fig. 10 it is thus not very clear what is indicated by the case  $G_B = 0$ ,  $C_3 = 1$ , since for  $G_B = 0$ ,  $R_f = 0$  and the case is independent of  $C_3$ . Is it the case without buoyancy effect in the  $k \sim \varepsilon$  model?

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## REPLY TO "COMMENTS ON 'MATHEMATICAL MODELLING OF BUOYANCY-INDUCED SMOKE FLOW IN ENCLOSURES"

THE INFLUENCE of buoyancy on the  $\varepsilon$  equation is indeed controversial. It is by no means clear that the suggestion of Rodi for  $S_{\varepsilon}$  is correct [1]. Consider, for example, the two definitions [I]

$$
R_{\rm f} = -\frac{G_{\rm B}}{G_{\rm k}},\tag{1}
$$

$$
R_{\rm f} = \frac{-G_{\rm BL}}{2(G_{\rm k} + G_{\rm B})} \tag{2}
$$

and the expression

$$
S_{\iota} = C_1 \frac{\varepsilon}{k} (G_k + G_B)(1 + C_3 R_f).
$$
 (3)

Using definition (1) we have

$$
S_{\epsilon} = C_1 \frac{\varepsilon}{k} \bigg[ G_k + G_B (1 - C_3) - C_3 \frac{G_B^2}{G_k} \bigg]. \tag{4}
$$

For vertical layers,  $C_3 = 0$ ,

$$
S_{\varepsilon} = C_1 \frac{\varepsilon}{k} (G_k + G_B). \tag{5}
$$

For horizontal layers,  $C_3 = 1$ ,

$$
S_z = C \frac{\varepsilon}{k} \left( \frac{G_k^2 - G_B^2}{G_k} \right) \tag{6}
$$

Using definition (2) we find that for vertical layers ( $G_{BL} = 0$ ) equation (5) still holds, but for horizontal ( $G_{BL} = 2G_B$ ) layers we have

$$
S_x = C_1 \frac{\varepsilon}{k} (G_k + G_B(1 - C_3)). \tag{7}
$$

There is a fundamental difference between equations (6) and (7), depending on the sign of  $G<sub>B</sub>$ . Thus equation (6) is always less than its value for the unmodified  $(k \sim \epsilon)$  model, while